

# Complete classification of the family of all finite sequences of points in a projective space

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## Introduction

Geometry in the sense of F. Klein can be seen as the theory of  $K$ -spaces [5]. The basic problems of this theory concern classification of figures. The classification is called complete if the classes are orbits. Any two elements in an orbit are called congruent.

